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Citation	Physical Review C,102(5),p.054318_1-054318_13
Text Version	Published Journal Article
URL	https://jopss.jaea.go.jp/search/servlet/search?5070863
DOI	https://doi.org/10.1103/PhysRevC.102.054318
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Structure of ³⁰Mg explored via in-beam γ -ray spectroscopy

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(Received 25 June 2020; accepted 9 October 2020; published 12 November 2020)

Background: In the "island of inversion," ground states of neutron-rich *sd*-shell nuclei exhibit strong admixtures of intruder configurations from the fp shell. The nucleus ³⁰Mg, located at the boundary of the island of inversion, serves as a cornerstone to track the structural evolution as one approaches this region.

Purpose: Spin-parity assignments for excited states in 30 Mg, especially negative-parity levels, have yet to be established. In the present work, the nuclear structure of 30 Mg was investigated by in-beam γ -ray spectroscopy mainly focusing on firm spin-parity determinations.

Method: High-intensity rare-isotope beams of ³¹Mg, ³²Mg, ³⁴Si, and ³⁵P bombarded a Be target to induce nucleon removal reactions populating states in ³⁰Mg. γ rays were detected by the state-of-the-art γ -ray tracking array GRETINA. For the direct one-neutron removal reaction, final-state exclusive cross sections and parallel momentum distributions were deduced. Multinucleon removal reactions from different projectiles were exploited to gain complementary information.

Results: With the aid of the parallel momentum distributions, an updated level scheme with revised spin-parity assignments was constructed. Spectroscopic factors associated with each state were also deduced.

Conclusions: Results were confronted with large-scale shell-model calculations using two different effective interactions, showing excellent agreement with the present level scheme. However, a marked difference in the spectroscopic factors indicates that the full delineation of the transition into the island of inversion remains a challenge for theoretical models.

DOI: 10.1103/PhysRevC.102.054318

I. INTRODUCTION

Changes from the canonical shell structure have been observed in neutron-rich unstable nuclei [1]. The unexpected deformation of the ground states of unstable Ne, Na, and Mg isotopes located around the classical magic number N =20 has attracted much attention since the 1970s. Triggered by the pioneering experiment that revealed the unexpectedly high binding energies in Na isotopes [2], anomalies were also found in the binding energies of Ne and Mg isotopes [3,4]. The low excitation energies of the first excited 2⁺ states [5–7] and the large collectivity in ³²Mg [8] have added experimental evidence for the disappearance of the N = 20magic number. In the shell-model picture, the disappear ance of magicity in this region is driven by the reduction of the effective single-particle energy gap between the *sd* and *pf* orbitals corresponding to the N = 20 gap [1,9,10]. This leads to increased contributions of excitations across the gap, e.g., two-particle two-hole (2p2h) configurations, in the ground states of these nuclei. The region where these unusual intruder configurations are dominant in the ground states was named the "island of inversion" [11]. This region has provided a rich testing ground for the modeling of nuclear structure far away from stability and particularly the evolution of the shell structure as a function of proton and neutron number.

The full delineation of the reasons for the emergence of the island of inversion is still underway. For the Mg isotopes, the characteristics of the ground state of ³¹Mg were studied by hyperfine structure and β -NMR measurements. It was found that the ground state has an unexpected spin-parity of $1/2^+$, in contrast to the naïve expectation of $3/2^+$ based on the normal configuration, i.e., a single neutron hole in the $1d_{3/2}$

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orbital. Accordingly, the ground state is understood as having a particle-hole dominated intruder configuration, thus placing ³¹Mg on the border of the island of inversion [12]. To explore the onset of intruder configurations, one-neutron knockout measurements on ³⁰Mg and ³²Mg, respectively, leading to ²⁹Mg and ³¹Mg, were performed [13]. The measurements revealed that there is a significant increase in the fp-shell occupation at ³²Mg compared to ³⁰Mg, pointing to a substantial structural change with the addition of two neutrons. Another important facet of the transition into the island of inversion is shape coexistence, where different shapes appear in near-degenerate states in the same nucleus. Experimental indications for shape coexistence have been found in ³⁰Mg [14] and ³²Mg [15,16]. The ground state of ³⁰Mg is characterized as having an essentially normal, spherical configuration where all the active neutrons are confined to the sd shell (0p0h), while the excited 0^+ state is described as an intruder, deformed configuration where two neutrons are promoted across the N = 20 gap (2p2h). The situation is considered to be inverted for ³²Mg, but recent theoretical and experimental studies [16–19] suggested that the above-mentioned interpretation might be too simplified. In this context, it is important to establish a microscopic view of ³⁰Mg.

To date, much experimental effort has been devoted to investigating the structure of ³⁰Mg. Since the first observations of ³⁰Mg [20,21], excited levels in this nucleus have been investigated by β - γ measurements of ³⁰Na [5,22– 24]. Levels in ³⁰Mg were also studied by β -delayed oneneutron emission from ³¹Na and two-neutron emission from 32 Na [25–27]. From these studies, the 2^+_1 state was established at 1482 keV and the shape coexisting 0^+_2 state was identified at 1789 keV [14]. The measured monopole transition strength of $\rho^2(E0; 0_2^+ \rightarrow 0_1^+) = (26.2 \pm 7.5) \times 10^{-3}$ was moderate and interpreted as arising from a small mixing of configurations with very different deformation [14]. To investigate the ground-state collectivity, three Coulomb excitation measurements on ³⁰Mg have been performed [28-30]. The latest measurement employing "safe" Coulomb excitation gave a moderate collectivity of $B(E2; 0^+_1 \rightarrow 2^+_1) = 241(31) e^2 \text{ fm}^4$. Recently, in-beam γ -ray measurements on ³⁰Mg using the $^{14}C(^{18}O, 2p)^{30}Mg$ fusion-evaporation reaction [31] and the one-neutron knockout reaction from ³¹Mg [32] have been reported. These measurements proposed candidates for negative-parity states lying at unusually low excitation energy around 2.5 MeV. The negative-parity states are formed by promoting an odd number of neutrons from the sd shell to the higher-lying f p orbitals with opposite parity. Thus, the location of negative-parity states is particularly important to discuss the structural evolution approaching the island of inversion [1,33], as it is indicative of the effective size of the N = 20 gap. It should also be emphasized that these negative-parity candidates are lying at lower energies than those presently known in ³²Mg [34], located at the heart of the island of inversion, implying an unusual structural change taking place at ³⁰Mg. Moreover, these energies are at variance with shell-model calculations [31,32], posing a question concerning the available shell-model description of ³⁰Mg. A more detailed spectroscopic study for conclusive spin-parity assignments was thus demanded.

TABLE I. List of rare-isotope beams produced in the measurement. Their incident energies (MeV/nucleon), averaged intensities on target (s^{-1}), and purities (%) are shown together.

Secondary beam	³¹ Mg	³² Mg	³⁴ Si	³⁵ P
Energy	97.9	99.1	94.8	102.3
Intensity	2.1×10^{4}	6.1×10^{3}	5.2×10^{5}	2.3×10^{5}
Purity	28	34	66	29

In the present work, the one-neutron knockout reaction from ³¹Mg induced by a nuclear target was performed to enable firm spin-parity assignments to states in ³⁰Mg. Additionally, the two-neutron removal reaction from ³²Mg was employed to populate states in ³⁰Mg. This reaction will receive only a small contribution from direct knockout, and therefore a near-statistical population of states with some intruder contributions is expected. Multinucleon removal reactions starting from ³⁴Si and ³⁵P, both of which lie outside the island of inversion, are also exploited. In these fragmentationlike reactions, the level population is less sensitive to the nuclear structure, but high-spin states, possibly with the yrast nature, are known to be preferentially populated [35–38]. Along with the spectroscopic factors that can be deduced from the one-neutron knockout measurement, a new level scheme with updated spin-parity assignments serves as an important test to the shell model and furthers our understanding.

II. EXPERIMENTAL DETAILS

The rare-isotope beams were produced by fragmentation of a ⁴⁸Ca primary beam at 140 MeV/nucleon delivered by the Coupled Cyclotron Facility at the National Superconducting Cyclotron Laboratory at Michigan State University [39]. The primary beam impinged on a 846-mg/cm² thick ⁹Be production target, and the rare-isotope ions of interest were separated from other fragments and selectively transmitted through the A1900 fragment separator [40] with a momentum acceptance of 1.1%. An aluminum wedge degrader with a thickness of 300 mg/cm^2 was placed at the intermediate plane of the A1900 to purify the cocktail of the fragments. The secondary beams containing ³¹Mg, ³²Mg, ³⁴Si, and ³⁵P were directed onto a 375-mg/cm² thick ⁹Be reaction target to induce nucleon removal reactions to populate states in ³⁰Mg. The identification of incoming radioactive ions was accomplished by measuring the time-of-flight (TOF) between two plastic scintillators placed at the extended focal plane of the A1900 and the object position of the analysis beamline of the S800 spectrograph located just upstream of the reaction target. The beam energies, intensities, and purities are tabulated in Table I.

The reaction products, including ³⁰Mg, were transmitted to the S800 spectrograph [41] and identified by the TOF- ΔE method. The TOF was measured between two plastic scintillators located at the object position and the focal plane of the S800 spectrograph. This scintillator was also used to trigger the electronics and data acquisition in coincidence with the γ -ray detection. An ionization chamber installed in the S800 focal plane was used to provide the energy loss information



FIG. 1. Doppler-corrected add-back γ -ray spectra of ³⁰Mg taken from four different reaction channels. The red, green, blue, and cyan histograms respectively show the spectra obtained from the incoming projectiles of ³¹Mg, ³²Mg, ³⁵P, and ³⁴Si. Transitions observed in the one-neutron removal reaction from ³¹Mg are indicated by dashed lines and labeled with their energies. Transitions with energies of 1061(3), 1097(2), 2312(4), 2774(5), and 3883(9) keV are observed in multinucleon removal reactions and indicated by dotted lines.

 (ΔE) for the identification of the atomic number. The trajectories of the reaction products were tracked in the S800 focal plane by two cathode readout drift chambers, providing position and angle information [42]. The parallel momentum and the angle at the target position were reconstructed from the trajectory measurements in the focal plane by the inverse-map approach [43].

The reaction target was surrounded by the Gamma-Ray Energy Tracking In-beam Nuclear Array (GRETINA) [44,45] to detect prompt de-excitation γ rays emitted by the reaction products in-flight. The array consisted of seven modules of GRETINA at the time of the experiment. Each module houses four closely packed crystals of high-purity germanium. The electrodes on the crystal are segmented into 36 elements so that interaction points of a γ ray can be reconstructed on the sub-segment level by online pulse-shape decomposition. Four modules covered forward angles around 58°, while the rest were aligned on the 90° ring. The γ -ray interaction points from GRETINA together with the velocity and angle of the reaction product at the target position, reconstructed from the trajectory measurement in the S800, enabled the Doppler correction of γ rays on an event-by-event basis. In the present measurement, an energy resolution of 1.4% in FWHM was achieved. The leading contributions to the linewidth are the uncertainties in the γ -ray interaction position and the velocity at which γ rays are emitted [45]. The add-back procedure was used for the identification of peaks and the γ - γ analyses. The extraction of γ -ray intensities was accomplished without add-back.

III. ANALYSIS AND EXPERIMENTAL RESULTS

A. Level scheme

The large statistics collected in the present experiment allowed us to extend the previously known level scheme of ³⁰Mg. The Doppler-corrected γ -ray spectra recorded in coincidence with residual ³⁰Mg nuclei obtained in the different

reaction channels, i.e., the one-neutron knockout reaction from ${}^{31}Mg$ and the multinucleon removal reactions from ${}^{32}Mg$, ${}^{34}Si$, and ${}^{35}P$, are shown in Fig. 1. The Doppler correction was performed with the mid-target velocity of the residue. The observed peaks are tabulated in Table II. The most prominent peak, observed at 1482 keV, corresponds to the $2^+_1 \rightarrow 0^+_1$ transition. The shoulderlike structure around 305 keV, which appears most prominently in one-neutron knockout, is attributed to the $0^+_2 \rightarrow 2^+_1$ transition. Since the 0_2^+ has a long half-life of 3.9(4) ns [26], the γ -ray emission takes place significantly downstream of the target and thus the $0^+_2 \rightarrow 2^+_1$ transition does not produce a clear peak in the spectrum. The transition energy and lifetime of this γ ray was not determined in this work, as the experiment was not designed for measurements of such a long-lived state. The peaks at 804, 956, 985, 1670, 1820, 1897, 1979, and 3541 keV observed in the one-neutron knockout reaction confirm the results of the previous measurement [32].

Selected γ -ray spectra from the γ - γ coincidence analysis are displayed in Fig. 2. Based on these observed coincidences, an updated level scheme has been constructed, as shown in Fig. 3. The present level scheme agrees with those constructed in previous studies [23,24,32]. The 1670-keV transition, which could not be placed in the level scheme in the previous one-neutron knockout measurement [32], was found to feed the state at 3540 keV, pointing to the existence of a new state at 5210 keV. The 2057-keV transition is assumed to depopulate the state at 3540 keV, guided by β - γ measurements [23,24]. The 804- and 881-keV transitions feed the state at 3379 keV, and these branches are consistent with the level scheme proposed in the previous fusion-evaporation experiment [31]. Part of the level scheme proposed in Ref. [31], especially the $5311 \rightarrow 4357 \rightarrow 2541 \rightarrow 1481 \rightarrow g.s.$ cascade, is at variance with the present results, and the presence of a negative-parity state at 2541 keV is not supported. Even though the states at 4260 and 4258 keV lie close to each other in energy, these two states must be different, as the ratio of

TABLE II. Observed γ -ray energies for the one-neutron knockout reaction from ³¹Mg and their placements in ³⁰Mg. Intensities relative to the prompt component of the 1482-keV transition in the one-neutron knockout spectrum are also indicated. The energies are shown in units of keV. In cases where the present statistics does not allow for γ - γ coincidences, the placements of transitions into the level scheme are adopted from Ref. [24] and shown in the parentheses (see text for details). The quoted uncertainties of the relative intensities show the statistical contributions.

Transition energy ^a	Placement	Relative intensity
305	$1788 \rightarrow 1482$	26.8(17) ^b
373(1) ^c		0.9(1)
804(1)	$4183 \rightarrow 3379$	2.8(1)
881(1)	$4260 \rightarrow 3379$	1.6(1)
956(1)	$4258 \rightarrow 3302$	10.2(1)
985(1)	$2467 \rightarrow 1482$	18.0(2)
1482(2)	$1482 \rightarrow 0$	$100.0(2)^{d}$
1670(3)	$5210 \rightarrow 3540$	2.7(1)
1820(3)	$3302 \rightarrow 1482$	24.3(2)
1897(3)	$3379 \rightarrow 1482$	9.9(2)
1979(3)	$3461 \rightarrow 1482$	21.5(2)
2057(3)	$3540 \rightarrow 1482$	2.6(1)
2219(5)	$(4683 \rightarrow 2466)$	0.6(1)
2453(4) ^c		1.3(1)
2618(12)	$(5095 \rightarrow 2466)$	0.7(2)
2648(11) ^c		0.9(2)
3200(5)	$(4683 \to 1482)$	2.7(2)
3431	$(5897 \rightarrow 2466)$	1.9(2)
3541(5)	$3540 \rightarrow 0$	12.7(2)
3625	$(5414 \to 1788)$	2.4(2)
3930	$(5414 \rightarrow 1482)$	1.6(2)
4293(7) ^c		1.9(1)
4415	$(5897 \to 1482)$	1.4(2)
4582	$(6064 \rightarrow 1482)$	0.4(2)
4967	$(4967 \rightarrow 0)$	0.4(2)
5022	$(5022 \rightarrow 0)$	1.4(2)
5095	$(5095 \rightarrow 0)$	0.8(2)
5414	$(5414 \rightarrow 0)$	2.7(2)

^aValues without uncertainties are taken from the β -decay study of Ref. [24].

^bAn additional systematic uncertainty of 10% arising from the halflife determination (3.9(4) ns [26]) also contributes.

^cUnplaced transitions.

^dThe intensity of the 1482-keV transition includes only the prompt component.

the 881-keV and 956-keV γ -ray intensities, depopulating the two states, strongly depends on the reaction channel. It is also found that the momentum distributions of the reaction residue gated on these two transitions are distinct (see Sec. III C for details).

B. Cross sections

For the one-neutron knockout reaction, the inclusive cross section to all bound states was determined to be 97(3) mb. The target thickness tolerance (1%) and the fluctuation in the secondary beam composition (3%) contribute to the



FIG. 2. Background-subtracted projections of the γ - γ coincidence matrices created by gating on different transitions. Peaks are labeled by their transition energy in keV. (a–g) To gain statistics, the γ - γ matrices of the one-neutron knockout reaction from ³¹Mg and the two-neutron removal reaction from ³²Mg are added. (h, i) The γ - γ matrices of the multinucleon removal reactions from ³⁴Si and ³⁵P are added.

quoted uncertainty. The present result compares well with the previously measured value of 90(12) mb [32], performed at a lower beam energy with a carbon target.

To deduce the exclusive cross section associated with each state, the observed Doppler-corrected γ -ray spectrum was fitted by a combination of GRETINA response functions generated by Monte Carlo simulations [46], yielding the γ -ray intensities (see Fig. 4). In addition to the transitions from the de-excitation of the residual nucleus, a continuous prompt γ -ray background is commonly observed in in-beam measurements. A double exponential was used to account for this contribution. Discrete γ -ray peaks observed in the laboratory-



FIG. 3. Proposed level scheme for ³⁰Mg from the present work. Excitation energies in keV, spins and parities are shown beside the levels. The spin-parity assignments are discussed in Sec. III C. A doublet is proposed at 3461 keV (see text for details).



FIG. 4. Doppler-corrected γ -ray spectra without add-back (black) for incoming beams of (a–c) ³¹Mg and (d) ³⁵P compared to the best-fit spectra obtained from simulations (red). Individual response functions are indicated by the green histograms. The response function for the delayed 305-keV transition is highlighted in blue. The gray solid line denotes background contributions (see text for details). The green shaded area in panels (c) and (d) represents the sum of the Compton-scattering components of all higher-lying peaks.

TABLE III. Experimental cross sections and spectroscopic factors. The orbital from which the neutron was removed is shown in the second column. The quoted uncertainties include systematic contributions propagating from the inclusive cross section and γ -ray detection efficiency (assumed to be 3%).

$E_{\rm x}$ (keV)	Orbital	$\sigma_{\rm exp}$ (mb)	$\sigma_{\rm sp}$ (mb)	$C^2 S_{exp}$
0	$2s_{1/2}$	17.2(30) ^a	52.1	0.33(6) ^a
1482	$1d_{3/2}$	10.2(5)	22.0	0.46(2)
1788	$2s_{1/2}$	13.8(19)	35.0	0.39(5)
2467	$1d_{3/2}$	8.4(4)	19.8	0.43(2)
3302	$1f_{7/2}$	7.9(4)	17.1	0.46(2)
3379	,	3.1(2)		
3461 ^b	$1d_{3/2}$	12.0(5)	18.0	0.67(3)
3461°	$1d_{3/2}$	5.8(6)	18.0	0.32(3)
	$2p_{3/2}$	6.2(6)	22.7	0.27(3)
3540	$2p_{3/2}$	6.2(3)	22.5	0.27(1)
4183	/-	1.5(1)		
4258	$1 f_{7/2}$	5.7(3)	16.1	0.35(2)
4260	5.7=	0.9(1)		
5210	$2p_{3/2}$	1.5(1)	18.9	0.08(1)
Others ^d	1 3/2	8.4(5)		
Inclusive		97 (3)		

^aThese values should be seen as upper limits.

^bA single state is assumed.

^cA doublet is assumed.

^dThe sum of the states at 4683, 4967, 5022, 5095, 5414, 5897, and 6064 keV. The placement in the level scheme is adopted from Ref. [24].

frame spectrum, arising from neutron-induced reactions on germanium crystals, as well as surrounding materials like the aluminum beam pipe and the aluminum detector housing, were Doppler-shifted and added to the fit function. The γ -ray intensities of the peaks lying above 600 keV were obtained from a single fit to the spectrum. The low-energy part of the spectrum, around the delayed 305-keV transition, was fitted separately with the fixed Compton-scattering components of the higher-lying peaks above 600 keV to better model the background contribution. The 305-keV response function was generated with a fixed half-life of 3.9 ns. The resulting γ -ray intensities, tabulated in Table II, were then corrected for the feeding based on the level scheme constructed in the present work. Some of the transitions could not be placed in the level scheme in the present $\gamma - \gamma$ analysis, but in some cases the level scheme constructed in a previous β -decay measurement [24] could be used to determine the feeding contributions. The exclusive cross sections are presented in Table III and Fig. 7. The ground-state cross section was obtained by subtracting the cross section to all excited states from the inclusive cross section. The unplaced transitions listed in Table II, with the summed intensity corresponding to a cross section of 2.5(2)mb, were not taken into account when calculating the exclusive cross sections.

The inclusive cross section for the two-neutron removal reaction from ³²Mg was determined to be 108(2) mb, a larger value than in one-neutron knockout. Similar trends are observed, for example, in Ref. [47]. The absolute cross sections



FIG. 5. Population strengths in the multinucleon removal reactions from (a) ${}^{32}Mg$, (b) ${}^{34}Si$, and (c) ${}^{35}P$ relative to those of ${}^{31}Mg$ (see Fig. 7 for the exclusive cross sections). Candidates for the high-spin states at 3379, 4183, and 4260 keV are highlighted in yellow.

for the multinucleon removal reactions from ${}^{34}Si$ and ${}^{35}P$ could not be deduced, because the residual ${}^{30}Mg$ nuclei were at the edge of the acceptance of the S800. The γ -ray spectra for the two-neutron and multinucleon removal reactions were analyzed in the same manner as the spectrum obtained for the knockout reaction from ${}^{31}Mg$. The relative population strengths are shown in Fig. 5.

C. Spin-parity assignments

The spin-parity assignments are primarily based on the momentum distributions of the knockout residue ³⁰Mg. The parallel momentum distribution recorded in coincidence with γ rays were then corrected for the feeding, assuming the present level scheme of Fig. 3. In Fig. 6, the measured distributions are compared with reaction calculations based on the eikonal and sudden approximations. The theoretical approach adopted here is commonly used in studies of one-nucleon knockout reactions induced by a nuclear target and is well documented [48,49]. The parallel momentum distributions can be calculated from the residue- and neutron-target eikonal S matrices, generated using double- and single-folding optical limit of Glauber's multiple scattering theory, respectively. As input to the calculation, densities of the residue and the target are required. Following the approach outlined in Refs. [50,51], the density of ³⁰Mg is taken from a Skyrme Hartree-Fock (HF) calculation using the SkX parameter set [52], while the density of the target nucleus ⁹Be is parameterized by a Gaussian with an RMS radius of 2.36 fm. The removed-neutron radial wave functions, the one-nucleon overlaps, are calculated with the well-depth prescription where the parameters of a Woods-Saxon-plus-spin-orbit potential are constrained by the RMS radii of the orbitals from the spherical HF calculation. The model calculations are folded with the momentum distribution of the unreacted beam of ³¹Mg after passing through the target $(140 \,\mathrm{MeV}/c \text{ in FWHM})$, to account for the broadening due to the momentum profile of the incoming beam and straggling effects in the target. The theoretical momentum distributions are normalized to the measured counts



FIG. 6. Parallel momentum distributions extracted from the experimental data compared with the reaction model calculations. The calculations assume knockout from the $2s_{1/2}$ (red), $1d_{3/2}$ (pink), $1f_{7/2}$ (blue), and $2p_{3/2}$ (cyan) orbitals. The yellow data points in panel (g) represent the 4260-keV momentum distribution. See text for details.

in the momentum region 12.12-12.56 GeV/c. The lower limit is chosen to avoid the influence of the low-momentum tail component, which cannot be described by the reaction model. In the following, spin-parity assignments to the observed states in 30 Mg are discussed.

The states at 1482 and 1788 keV have been previously assigned as the 2_1^+ and 0_2^+ states, respectively. The measured momentum distributions, shown in Figs. 6(a) and 6(b), are compatible with knockout from the $1d_{3/2}$ and $2s_{1/2}$ orbitals, respectively. It should be noted that the present data did not allow for the clear extraction of the ground-state momentum distribution. This implies that there are remaining unobserved weak transitions that feed the ground state.

For the 2467-keV state, the present data clearly favor knockout from the $1d_{3/2}$ orbital [the reduced χ^2 is 4.9 (60.0) for $1d_{3/2} (2p_{3/2})$], in contrast with the conclusion drawn in the previous study where a 2⁻ assignment was made [32]. This state was originally discussed as a candidate for the 2^+_2 state [26], and in the present study, a 2⁺ assignment is firmly made.

For the state at 3461 keV, the observed momentum distribution shows a narrow and almost symmetric shape. This is not compatible with the 4^+ assignment previously given [31], as the spin coupling of the $1/2^+$ ground state in ³¹Mg with a neutron in the *sd pf* orbitals does not allow a 4^+ state to be populated directly. The momentum distribution suggests

knockout from the $1d_{3/2}$ orbital, but the reduced χ^2 [14.2 (43.1) for $1d_{3/2} (2p_{3/2})$] is higher than in other cases. This may be explained by the presence of two near-degenerated states. A β -decay study proposed a doublet of states emitting 1978and 1980-keV γ rays [53], but in the present experiment it is not possible to disentangle the populations of these states because of the limited energy resolution. Nevertheless, a fit to the observed momentum distribution allows for the extraction of each contribution if assuming $1d_{3/2}$ and $2p_{3/2}$ components. The resulting cross sections are 5.8(6) mb and 6.2(6) mb for the $1d_{3/2}$ and $2p_{3/2}$ orbitals, respectively. One might assume a $2s_{1/2}$ component instead of $2p_{3/2}$, but such a state with a possible spin-parity of 1⁺ occurs only above 4.8 MeV according to shell-model calculations (see Sec. IV A).

Because of the spin coupling of the ³¹Mg ground state and the pf orbitals, only a single orbital contributes to the momentum distribution of a negative-parity state with $J^{\pi} = 1^{-}-4^{-}$. The removal of a neutron from the $1 f_{7/2}$ orbital allows for the population of 3⁻ or 4⁻ states, and the 3302-keV momentum distribution supports knockout from this orbital. Given the observed sole branch to the 2_1^+ state, a spin-parity assignment of 3⁻ with an E1 transition is most likely. The 4258-keV momentum distribution also undoubtedly shows knockout from the $1 f_{7/2}$ orbital. This state decays via the 956-keV transition to the 3^- state. With the nonobservation of decay branches to the 2^+ states, this state likely has a spin-parity of 4^- . The removal of a $2p_{3/2}$ neutron can lead to either 1⁻ or 2⁻ states. For the 3540-keV state, the momentum distribution is compatible with knockout from the $2p_{3/2}$ orbital, and a 1⁻ assignment is proposed here, because of the observation of the ground-state decay. This spin-parity assignment reasonably explains the branching ratio to the 2^+_1 state (γ -ray intensity 20(1)% with respect to the ground-state transition). The newly found 5210-keV state is also characterized by knockout from the $2p_{3/2}$ orbital, and guided by the absence of the groundstate decay, a spin-parity of 2^- is suggested.

The preferred population of high-spin states in fragmentationlike reactions [35–38] serves as a qualitative tool to identify such states. As can be seen in Fig. 5, relative enhancements of the cross sections for the states at 3379, 4183, and 4260 keV compared to the direct one-neutron knockout reaction from ³¹Mg are observed in the multinucleon removal reactions, suggesting that these states likely have high spins $(J \ge 4)$. Furthermore, the corresponding momentum distributions in one-neutron knockout show shifted centroids (see Fig. 6(g) for the example of the 4260-keV state). This implies that these states are populated by nondirect one-neutron removal pathways [54] such as the evaporation of one neutron following inelastic excitation. The 3379-keV state was assigned as a 4^+ state in a previous study [31], and the present data add to the evidence for this assignment. It is worthwhile to emphasize that the 4_1^+ state at 3379 keV built on top of the 2_1^+ state leads to $R_{42} = 2.3$, which is close to the vibrational limit. A candidate for an yrast state with J = 5 [31] was observed at 4183 keV in the present measurement. Similarly, as can be seen in Fig. 6(g), the present data suggest a high-spin character of the 4260-keV state. The different momentum distributions for the 4258- and 4260-keV states prove that these are two different states.

D. Spectroscopic factors

Given a set of theoretical spectroscopic factors, the theoretical cross section for a final state J_f^{π} is computed as the sum of contributions from each single-particle orbital with quantum numbers nl j

$$\sigma_{\rm th} = \sum_{nlj} \left(\frac{A}{A-1}\right)^N C^2 S(J_f^{\pi}, nlj) \sigma_{\rm sp} [S_n + E_{\rm x}(J_f^{\pi}), nlj],$$
(1)

where σ_{sp} is the single-particle cross section taken from the reaction calculation performed in the same framework as that described in the previous section. The σ_{sp} is calculated at the effective neutron separation energy $S_n + E_x(J_f^{\pi})$. The factor $[A/(A-1)]^N$, with N being the major oscillator quantum number [2 (3) for the sd (pf) orbitals], represents the centerof-mass correction to the shell-model spectroscopic factors. The experimental spectroscopic factors presented in Table III are calculated as the ratio of the measured cross section to the calculated σ_{sp} . For 2⁺ states, the experimental spectroscopic factors are deduced assuming a pure $1d_{3/2}$ contribution. According to shell-model calculations detailed in Sec. IV A, the $1d_{3/2}$ component dominates over $1d_{5/2}$ for low-lying 2⁺ states.

The large deduced cross section populating the ground state leads to a sizable spectroscopic strength of 0.33(6) by $2s_{1/2}$ neutron removal. This value should be seen as an upper limit, because of the presence of unplaced or unobserved transitions that feed the ground state. Such overestimation of exclusive cross sections for low-lying states is inevitable in γ -tagged measurements. A sizable spectroscopic factor of 0.39(5) obtained for the 0^+_2 state is in line with a simple expectation that the 0^+_2 state in 30 Mg is characterized by substantial overlap with the intruder-dominated, deformed ground state of ³¹Mg. With the revised spin-parity assignment for the 2467-keV state, the corresponding spectroscopic factor was determined to be 0.43(2). The existence of a doublet of states is proposed at 3461 keV, and the spectroscopic factors for the two (unresolved) states are 0.32(3) $(1d_{3/2})$ and 0.27(3) $(2p_{3/2})$. The observed large contributions from the negative-parity orbitals are the direct consequence of the intruder-dominated character of the ³⁰Mg ground state. This point is revisited in the next section.

IV. DISCUSSION

A. Comparison to shell-model calculations

To assess the theoretical description of ³⁰Mg, large-scale shell-model calculations were performed using the SDPF-M [55] and EEdf1 [18] effective interactions. The former interaction, developed in 1999, has been traditionally used in studies of island-of-inversion nuclei. The model space of the interaction comprises of the full *sd* shell and the lower half of the *fp* shell ($1f_{7/2}$ and $2p_{3/2}$) for both neutrons and protons. The two-body matrix elements (TBMEs) and the single-particle energies (SPEs) were empirically adjusted to reproduce selected experimental observables. The EEdf1 interaction was developed most recently with the model space extending to the full *fp* shell. This interaction is



FIG. 7. Comparison of (a) experimental cross sections to those obtained from shell-model calculations using different interactions, (b) SDPF-M, (c) modified SDPF-M, and (d) EEdf1. States characterized by $2s_{1/2}$, $2p_{3/2}$, $1d_{3/2}$, and $1f_{7/2}$ are respectively shown in red, cyan, pink, and blue. The experimental ground-state cross section should be seen as an upper limit. Two close-lying states that cannot be resolved in the present experiment likely contribute for the experimental cross section of the 3461-keV state shown in gray (see text for details). The yellow data points in panel (a) are for the observed candidates for the high-spin states. The yrast 4⁺ states are indicated by the yellow arrows.

different from SDPF-M by construction in that the TBMEs are microscopically derived. The Kuo-Krenciglowa method and the Entem-Machleidt QCD-based nucleon-nucleon interaction are used for the derivation of TBMEs, while the SPEs are fitted to reproduce selected experimental data. The calculations were performed with the code KSHELL [56]. The SDPF-M result is obtained from the full diagonalization, whereas the number of excitations is restricted up to 6p6h for the EEdf1 interaction, due to computational limitations. The calculated levels and their cross sections are compared with those measured in Fig. 7. The overall level structure, especially the locations of the 2_1^+ , 0_2^+ , and 2_2^+ states, as well as the negative-parity levels, are remarkably well reproduced by both calculations. The predicted excitation energies of the 4_1^+ state using the SDPF-M and EEdf1 interactions are 3.47 and 3.16 MeV, respectively, showing good agreement with the experiment (3379 keV). We note that the recently developed SDPF-U-MIX interaction [17], also well reproduces the experimental level scheme (see Ref. [32]).

In addition to the excitation energies, the calculated electromagnetic transition strengths between low-lying states show good agreements with the experimental data. As shown in Table IV, the theoretical and experimental strengths compare well for the $2_1^+ \rightarrow 0_1^+$ and $0_2^+ \rightarrow 2_1^+$ transitions. Experimentally, a substantial *M*1 component of the $2_2^+ \rightarrow 2_1^+$

TABLE IV. Comparison of theoretical and experimental transition strengths. Adopted effective charges are $(e_p, e_n) = (1.3, 0.5)e$ for SDPF-M [55] and $(e_p, e_n) = (1.25, 0.25)e$ for EEdf1 [18]. The strengths are taken to be in units of e^2 fm⁴ (*E*2) and μ_N^2 (*M*1).

Transition	SDPF-M	EEdf1	Experiment
$\overline{0^+_1 \rightarrow 2^+_1}$	332	285	241(31) [30]
$0^+_2 \rightarrow 2^+_1$	38	51	53(6) [14]
$2^+_2 \rightarrow 2^+_1$	1.8 (E2)	1.0 (E2)	>123 ^a
	0.16 (<i>M</i> 1)	0.19 (<i>M</i> 1)	

^aThe lower limit is given by the upper limit on the lifetime when a pure E2 character is assumed [26].

transition was suggested, following the upper limit on the 2^+_2 level half-life of 5 ps [26]. The calculations indicate that the $2^+_2 \rightarrow 2^+_1$ transition has strong mixing of *M*1. Simulations show that a half-life of 5 ps leads to a slight shift of the 985-keV peak by 1 keV in the Doppler-corrected spectrum produced with the mid-target velocity. The observation of the peak at 985 keV is, therefore, in line with the above-mentioned upper limit.

Unlike the level structure and the transition strengths, exclusive cross sections indicated by bars in Fig. 7 show marked differences depending on the interaction. As the SDPF-M interaction does not reproduce the correct level ordering of ³¹Mg [18], the wave function of the lowest $1/2^+$ state is taken as the ³¹Mg ground state for the calculation of the spectroscopic factors. We note that the EEdf1 interaction correctly reproduces the ground-state spin-parity, and the calculation and the experimental level scheme of ³¹Mg agree well [57]. As can be seen in Fig. 7, the comparison with the measurement does not allow for a definitive choice between the shell-model calculations; the spectroscopic factors associated with the negative-parity states are quantitatively better reproduced in the EEdf1 calculation, whereas the large spectroscopic factor for the 2^+_2 state is only reproduced by the SDPF-M interaction.

We also note that the theoretical inclusive cross section calculated with the SDPF-M interaction amounts to 91 mb with a theoretical uncertainty of 13 mb estimated by varying the S_n by ± 500 keV. When using the EEdf1 interaction, the number of states calculated is limited due to the high computational cost and therefore the inclusive cross section could not be computed. The experimental inclusive cross section for direct knockout is estimated to be 91(3) mb by subtracting the cross sections of the 3379-, 4183-, and 4260-keV states, populated by nondirect one-neutron removal, from the measured inclusive cross section. According to the systematics of Ref. [51], the ratio of the experimental to the theoretical direct-knockout inclusive cross sections is expected to be around 0.9. The present result conforms to this expectation within the uncertainty margin.

To see the correlation between the interaction and the predicted spectroscopic factors, calculations with modified SPEs have been performed based on the SDPF-M interaction [58–60]. The overestimated $1f_{7/2}$ spectroscopic factor is mitigated by reducing the energy spacing between the $1f_{7/2}$ and $2p_{3/2}$ orbitals corresponding to the N = 28 gap. This



FIG. 8. T-plots for the 0_1^+ , 2_1^+ , 0_2^+ , and 2_2^+ states in ³⁰Mg and the lowest $1/2^+$ state in ³¹Mg produced using the SDPF-M and EEdf1 interactions. The contour plots show the potential energy surfaces, while the circles indicate the deformed Slater determinants (see text for details).

is demonstrated in Fig. 7, where "SDPF-M-mod" represents the calculation with the single-particle energies of the $1f_{7/2}$ $(2p_{3/2})$ orbitals raised (lowered) by 0.5 MeV. This modification reduces the $1f_{7/2}$ neutron occupancy in the ³¹Mg ground state by 14%, leading to smaller $1f_{7/2}$ spectroscopic factors. This indicates that the spectroscopic strengths of the negativeparity states are also sensitive to the effective shell-gap size. Note that a lowering of the $2p_{3/2}$ SPE alone [58–60] also leads to a reduced $1f_{7/2}$ occupancy, but results in a smaller 2^+_2 spectroscopic strength.

To further differentiate the two interactions used in the present work, the low-lying states in $^{30}\text{Mg},$ i.e., the $0^+_1,\,2^+_1,$ 0_2^+ , and 2_2^+ states, were analyzed by the T-plot technique [61] to explore the nature of the underlying wave functions. The plots, in Fig. 8, show the potential energy surface obtained by a constrained HF calculation using the shellmodel interactions. The circles in the plots represent deformed Slater determinants in the Monte Carlo shell model (MCSM) framework [62], and their size is proportional to the overlap between the MCSM eigenstate and the deformed Slater determinant. With this approach, the intrinsic deformation of each state is visualized. As can be seen in Fig. 8, the two interactions predict very different structures for ³⁰Mg despite the similar level schemes, but the shape-coexisting feature persists; the circles are localized both in the weakly deformed and strongly prolate-deformed sides. For the SDPF-M cal-



FIG. 9. Systematics of levels in N = 18 isotones. Level data are taken from the ENSDF database, while the levels in ³⁰Mg are taken from the present analysis. The lowest 1⁻ (3⁻) states are connected by dashed (dotted) lines. Negative-parity (positive-parity) states are shown in blue (red).

culation, the 0_1^+ state exhibits a weakly deformed shape, indicated by the clustering of large circles in the region of $\langle Q_0 \rangle \approx 30 \,\mathrm{fm}^2$ and $\langle Q_2 \rangle \approx 10 \,\mathrm{fm}^2$, while the 0_2^+ is governed by strongly deformed configurations where the circles are localized around $\langle Q_0 \rangle \approx 70 \text{ fm}^2$. The 2_1^+ and 2_2^+ states are characterized by a higher degree of shape mixing. Here, it is worth noting that the calculated spectroscopic factors may be intuitively understood by the T-plots. The ground state of ³¹Mg is prolate-deformed, and the 0_1^+ (0_2^+) states are characterized by weakly (strongly) deformed configurations, thus yielding small (large) overlaps and spectroscopic factors. The spectroscopic factors of the 2_1^+ and 2_2^+ states with similar magnitudes are understood by large shape fluctuations. In the EEdf1 results, it is seen that shape mixing is more pronounced in the 0_1^+ and 0_2^+ states. Moreover, the shape coexistence in the 2_1^+ and 2_2^+ states is "inverted" with respect to the naïve expectation, i.e., the 2_1^+ state is dominated by deformed configurations while the 2_2^+ state is close to spherical.

Usually, excitation energies are used as a first test of theoretical calculations. The present results demonstrate that more detailed experimental information, such as spectroscopic factors, is required to further differentiate the models. The findings obtained here provide guidance for refinements of the interactions, and the new experimental information will serve as a benchmark towards the full description of the nuclear structure in and around the island of inversion.

B. Transition into the island of inversion

Systematics of the level structure along the N = 18 isotones are displayed in Fig. 9. It is seen that, going from ³⁸Ca to ³²Si, the 1⁻ states stay constant around 6 MeV and the 3⁻ states continue to rise steadily up to 5.3 MeV, but a rapid



FIG. 10. Comparison of summed experimental spectroscopic factors to neutron occupancies calculated for (a–c) the $1f_{7/2}$ and (d–f) the $2p_{3/2}$ orbitals. The filled region shows calculated spectroscopic factors summed up to S_n . The calculated values are corrected for the $[A/(A-1)]^N$ factor. The triangle represents the sum including the contribution of $2p_{3/2}$ at 3461 keV where a doublet is proposed.

lowering of the excitation energies is observed at ³⁰Mg. This is interpreted as a precursory structural change approaching the island of inversion. If one assumes a naïve 1p1h excitation in the framework of the shell model, then the excitation energy of the negative-parity state can be related to the gap size between effective single-particle orbitals. A 1⁻ state is formed by promoting one neutron from the $1d_{3/2}$ orbital to $2p_{3/2}$. Therefore, the observed drop of the 1⁻ states could be interpreted as driven by the reduced gap between the $1d_{3/2}$ and $2p_{3/2}$ orbitals, thus indicating the shell evolution that is considered to be responsible for the appearance of the island of inversion. This behavior is found to coincide with the lowering of the effective single-particle energy of the $2p_{3/2}$ orbital with respect to $1d_{3/2}$ both in the SDPF-M and EEdf1 interactions. A drop of excitation energy is also seen for the 3⁻ states, but the underlying configuration is not as simple as the 1^- states, as a 3⁻ state can be formed by promoting one neutron from the $1d_{3/2}$ orbital to both the $1f_{7/2}$ and $2p_{3/2}$ orbitals. This drop in excitation energy is analogous to the N = 8 chain where the sudden lowering of the 1^{-} state is observed at ¹²Be [33].

To track the evolution of the fp-shell occupancy approaching the island of inversion, the summed spectroscopic factors associated with the $1f_{7/2}$ and $2p_{3/2}$ orbitals are shown in Fig. 10. For ³¹Mg, the spectroscopic factors populating negative-parity states in ³⁰Mg were taken from the present work. Those of ³⁰Mg and ³²Mg were taken from a previous measurement of one-neutron knockout reactions [13]. The observed continuous transition expands the early concept of the island of inversion with sharp borders [11] and corroborates, in a quantitative manner, a gradual-transition scenario which has been theoretically predicted [55].

V. SUMMARY AND CONCLUSION

The structure of the neutron-rich nucleus 30 Mg located at the boundary of the island of inversion was studied in detail by in-beam γ -ray spectroscopy. To populate states in 30 Mg,

the one-neutron knockout reaction from ³¹Mg was primarily employed. Multinucleon removal reactions leading to ³⁰Mg were also studied to obtain additional information beneficial to construct an updated level scheme and to constrain the spins and parities of populated states. In the knockout reaction, the momentum distributions of the residual ³⁰Mg are characteristic of the angular momentum of the removed neutron. Together with the well-established reaction mechanism and its theoretical prescriptions, the momentum distributions were then used to assign spins and parities of the populated states. Spectroscopic factors for each state were also deduced based on the measured cross sections and reaction model calculations.

The location of the negative-parity states, which reflects the effective size of the N = 20 shell gap, was established. Contrary to previous studies, indications of negative-parity states at low excitation energies below 3 MeV were not found. Nevertheless, the drop of the excitation energy of the negativeparity states from Si (Z = 14) to Mg (Z = 12) pertains. The negative-parity states were strongly populated in the knockout reaction. In particular, the neutron knockout from the $2p_{3/2}$ orbital showed significant spectroscopic strength, corroborating the intruder-dominated configuration in the ground state of ³¹Mg. These experimental findings are interpreted as a precursory structural change approaching the island of inversion.

To gain more insight into the nuclear structure of 30 Mg, large-scale shell-model calculations have been performed. The updated level scheme is very well reproduced by the calculations, whereas the spectroscopic factors show large variations depending on the interaction used. It was also found that the picture of shape coexistence in 30 Mg largely depends on the interaction and is correlated with the calculated spectroscopic factors. The observed spectroscopic factors are not completely reproduced by the shell-model calculations using the SDPF-M and EEdf1 interactions for all states, implying the transition into the island of inversion is not fully captured in the present shell model.

To fully map the transition into the island of inversion, further detailed spectroscopic studies of nuclei in and around the island of inversion are needed. Transfer reactions starting from or leading to ³⁰Mg could be used to verify the predicted small spectroscopic factors between the two ground states, as the reactions are performed using the missing-mass method. Furthermore, multistep Coulomb excitation could shed more light on the shape coexistence and deformation in ³⁰Mg.

ACKNOWLEDGMENTS

We express our gratitude to the accelerator staff at NSCL for their efforts in beam delivery during the experiment. N.K. acknowledges support of the Grant-in-Aid for JSPS Fellows (No. 18J12542) from the Ministry of Education, Culture, Sports, Science, and Technology (MEXT), Japan. The shell-model calculations were enabled by the CNS-RIKEN joint project for large-scale nuclear structure calculations and were performed mainly on the Oakforest-PACS supercomputer. N.S., N.T., and Y.U. acknowledge support by MEXT and JIC-FuS as post-K priority issue 9 (No. hp180179, No. hp190160, and No. hp200130), "Program for Promoting Researches on

the Supercomputer Fugaku" (Simulation for basic science: from fundamental laws of particles to creation of nuclei), and the Multidisciplinary Computational Sciences Project of Tsukuba University (No. xg18i035). J.A.T. acknowledges support from the U.K. Science and Technology Facilities Council Grant No. ST/L005743/1. This work was supported by the U.S. Department of Energy (DOE), Office of Science,

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Office of Nuclear Physics, under Grant No. DE-SC0020451 and by the U.S. National Science Foundation (NSF) under Grant No. PHY-1306297. GRETINA was funded by the U.S. DOE, Office of Science. Operation of the array at NSCL is supported by the U.S. NSF under Cooperative Agreement No. PHY-1102511 (NSCL) and DOE under Grant No. DE-AC02-05CH11231 (LBNL).

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