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STUDY OF ELECTRIC PHENOMENA IN ENERGY
DUMPING OF LCT COIL

March 1980

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Study of Electric Phenomena in Energy Dumping of LCT Coil

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(Received January 30, 1980)

In IEA-LCT coil, electric phenomena in energy dumping were studied analytically and experimentally.

Protection resistance of the Japanese LCT coil is chosen as 0.1Ω considering the quenching voltage, so that temperature rise of the coil is no problem.

Energy dumping characteristic of the six-coil system is calculated under different conditions. It is concluded that simultaneous dumping of all the coils with the equivalent resistance values of protection is necessary.

Flashover voltage tests of the model in 4.2 K liquid helium, 4.2 K gas helium and 4.2 K boiling helium show margin in practical quenching voltage of the coil.

Keywords; Coil Quenching, Energy Dumping, Coil Protection, Superconducting Magnet, Insulating Voltage, Insulating Spacer, Temperature Rise

* On leave from Hitachi Wire and Cable Ltd.

LCT コイルのエネルギーダンピングに伴う電氣的現象に関する検討

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(1980年1月30日受理)

現在、設計および製作を進めているIEA-LCT コイルについて、コイル・クエンチに伴う電氣的諸問題を解析的および実験的に検討した。

わが国が製作するヘリウム浸漬冷却コイルでは、耐電圧の面からクエンチ保護抵抗 0.1Ω 選定し、それでコイル温度上昇の面でも問題がないことを確認した。

6個組合せコイル試験では1個のコイルがクエンチした場合、他の全てのコイルもダンピングする必要があり、その場合でも、コイル保護抵抗が互いに大きく相異するとダンピング電圧の上昇を招き、好ましくない。

ダンピング時発生電圧に対する巻線スペーサの絶縁耐力については、パンケーキ間絶縁を模擬した試験試料を製作し、液体ヘリウム、気体ヘリウム、ならびに液体ヘリウム中に気体ヘリウム気泡が発生した状態で絶縁破壊試験を行ない、実コイルについてはかなりの裕度があることが判明した。

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1. Introduction

IEA-LCT (Large Coil Task) has been started since 1977. In this project the six large scale superconducting magnets built by four international participants will be assembled at ORNL (Ork Ridge National Laboratory), where experimental coil tests are planned.¹⁾

In this project JAERI has been fabricating a pool-cooling coil with edge-wise pancake windings of Nb-Ti conductor.²⁾

This report describes calculation and experimental studies on electric phenomena due to energy dumping of LCT coil.

Table 1 shows the main parameters of the Japanese LCT coil.

2. Choice of the Resistance Value for the Japanese LCT Coil Protection

In this report, calculation is executed with the assumption that six coils have the same electric constants as those of the Japanese LCT coil. Electric parameters of the Japanese coil are listed in Table 2. With the coil arrangement shown by Fig. 1, the whole energy E_1 of No.1 coil is

$$E_1 = \frac{1}{2} L_0 I_1^2 + M_1 I_1 I_2 + M_2 I_1 I_3 + M_3 I_1 I_4 + M_2 I_1 I_5 + M_1 I_1 I_6$$

Calculated results are later summarized in Table 4 (Sec. 5.1), where 100 % current of each coil is assumed to be 10 kA.

In order to set the resistance value of the coil protection there are various conditions. We take the next conditions

We take the next conditions for LCT coil.

- (1) By ORNL LCT specification, the temperature rise of conductor during coil dumping shall be lower than 80 K in case of the Normal Operation, 100 K in case of the Extend Test (ALT, A etc.).
- (2) The Japanese LCT coil is operated by pool cooling system, so that a high voltage is not acceptable. The maximum voltage between the terminals should be below 1 kV.

Thus we chose 0.1 Ω of protecting resistance of the Japanese LCT coil.

3. Analysis of Current and Voltage during LCT Coil Dumping

3.1 General Solutions for Six Coil System

Currents of the coils during coil dumping, I_1, I_2, \dots, I_6 are generally written by the next expression.

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$$\begin{bmatrix} I_1 \\ I_2 \\ \vdots \\ \vdots \\ I_6 \end{bmatrix} = \begin{bmatrix} I_{11} & I_{12} & \dots & I_{16} \\ I_{21} & I_{22} & \dots & I_{26} \\ \vdots & \vdots & & \vdots \\ \vdots & \vdots & & \vdots \\ I_{61} & I_{62} & \dots & I_{66} \end{bmatrix} \begin{bmatrix} \exp(p_1 t) \\ \exp(p_2 t) \\ \vdots \\ \vdots \\ \exp(p_6 t) \end{bmatrix} \quad (1)$$

Coefficients $I_{11}, I_{12}, \dots, I_{66}$ shall be determined through unknown coefficient method by later equations (4) ~ (9), and

P_1, P_2, \dots, P_6 are roots of the next sixth equations.

$$\begin{vmatrix} L_{11}P+R_1 & L_{12}P & \dots & L_{16}P \\ L_{21}P & L_{22}P+R_2 & \dots & L_{26}P \\ \vdots & \vdots & & \vdots \\ L_{61}P & L_{62}P & \dots & L_{66}P+R_6 \end{vmatrix} = 0 \quad (2)$$

Where $L_{11}, L_{12},$ etc. are coefficients of induction in the six coil system and $R_1, R_2,$ etc. are protection resistances which are independently connected to that coils.

$R_k = 0$ in the equation (2) corresponds to no dumping of No. k coil. Equation (2), as far as $R \neq 0$, is transformed to the next eigen value equation.

$$\begin{vmatrix} \frac{L_{11}}{R_1} - \frac{1}{-p}, \frac{L_{12}}{R_1} & \dots & \frac{L_{16}}{R_1} \\ \frac{L_{21}}{R_2}, \frac{L_{22}}{R_2} - \frac{1}{-p} & \dots & \frac{L_{26}}{R_2} \\ \vdots & & \vdots \\ \frac{L_{61}}{R_6}, \frac{L_{62}}{R_6} & \dots & \frac{L_{66}}{R_6} - \frac{1}{-p} \end{vmatrix} = 0 \quad (3)$$

Coefficients $I_{11}, I_{12}, \dots, I_{66}$ are determined by the following 36 simultaneous equations.

$$\begin{bmatrix} P_1L_{11}+R_1 & P_1L_{12} & \dots\dots\dots & P_1L_{16} \\ P_1L_{21} & P_1L_{22}+R_2 & & P_1L_{26} \\ \vdots & \vdots & & \vdots \\ P_1L_{61} & P_1L_{62} & & P_1L_{66}+R_6 \end{bmatrix} \begin{bmatrix} I_{11} \\ I_{21} \\ \vdots \\ I_{61} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (4)$$

$$\begin{bmatrix} P_2L_{11}+R_1 & P_2L_{12} & \dots\dots\dots & P_2L_{16} \\ P_2L_{21} & P_2L_{22}+R_2 & & P_2L_{26} \\ \vdots & \vdots & & \vdots \\ P_2L_{61} & P_2L_{62} & & P_2L_{66}+R_6 \end{bmatrix} \begin{bmatrix} I_{12} \\ I_{22} \\ \vdots \\ I_{62} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (5)$$

$$\begin{bmatrix} P_3L_{11}+R_1 & P_3L_{12} & \dots\dots\dots & P_3L_{16} \\ P_3L_{21} & P_3L_{22}+R_2 & & P_3L_{26} \\ \vdots & \vdots & & \vdots \\ P_3L_{61} & P_3L_{62} & & P_3L_{66}+R_6 \end{bmatrix} \begin{bmatrix} I_{13} \\ I_{23} \\ \vdots \\ I_{63} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (6)$$

$$\begin{bmatrix} P_4L_{11}+R_1 & P_4L_{12} & \dots\dots\dots & P_4L_{16} \\ P_4L_{21} & P_4L_{22}+R_2 & & P_4L_{26} \\ \vdots & \vdots & & \vdots \\ P_4L_{61} & P_4L_{62} & & P_4L_{66}+R_6 \end{bmatrix} \begin{bmatrix} I_{14} \\ I_{24} \\ \vdots \\ I_{64} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (7)$$

$$\begin{bmatrix} P_5L_{11}+R_1 & P_5L_{12} & \dots\dots\dots & P_5L_{16} \\ P_5L_{21} & P_5L_{21}+R_2 & & P_5L_{26} \\ \vdots & \vdots & & \vdots \\ P_5L_{61} & P_5L_{62} & & P_5L_{66}+R_6 \end{bmatrix} \begin{bmatrix} I_{15} \\ I_{25} \\ \vdots \\ I_{65} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix} \quad (8)$$

$$\begin{bmatrix} I_{11} + I_{12} + \dots\dots\dots + I_{16} \\ I_{21} + I_{22} + \dots\dots\dots + I_{26} \\ \vdots \\ I_{61} + I_{62} + \dots\dots\dots + I_{66} \end{bmatrix} = \begin{bmatrix} I_{10} \\ I_{20} \\ \vdots \\ I_{60} \end{bmatrix} \quad (9)$$

Where $I_{10}, I_{20}, \dots\dots\dots I_{60}$ are currents just at the moment of the beginning of dumping in No.1, No.2, $\dots\dots\dots$ No.6 coil respectively.

Terminal voltage of each coil is given by the multiplication of each current and the protection resistance of that coil.

3.2 Simultaneous Dumping Whole Coils with the Same Dumping Time Constant

The normal resistance value in the superconducting winding is practically neglected in comparison with the protection resistance value R_p .

The discharge currents I of all coils with the same dumping constant are expressed by

$$I = I_0 \exp \left(- \frac{R_p}{L} \cdot t \right)$$

I_0 : Initial current (A)

t : Time after initiating discharge (sec)

$$\begin{aligned} L &= L_1 + 2M_1 + 2M_2 + M_3 \\ &= 2.972 \text{ H} \end{aligned}$$

$$R_p = 0.1 \ \Omega$$

$$L/R_p = 29.72 \text{ sec.}$$

Accordingly, the time constant of the system is 29.72 sec.

3.3 Current Characteristic with Different Dumping Resistance

As an example with different dumping resistances, calculations of the dumping current have been performed with the arrangement of Fig. 1, where the different resistances are alternatively connected. Because it may be expected that there exist plain effected modes in current by each other.

The numerical solution I of dumping current of No.1 coil for two typical cases are given as following.

$$\text{Case I; } R_1 = 0.1 \ \Omega, \quad R_2 = 0.25 \ \Omega$$

$$I_1 = 10\{1.3766 \exp(-0.03812t) - 0.3766 \exp(-0.1268t)\} \text{ kA}$$

$$\text{Case II; } R_1 = 0.1 \ \Omega, \quad R_2 = 1 \ \Omega$$

$$I_1 = 10\{1.3886 \exp(-0.04046t) - 0.3886 \exp(-0.478t)\} \text{ kA}$$

Examples of these two cases are shown in Fig. 2. If the difference of the coil protection resistance is so large as shown in an example for the

Case II, the dumping current value of the coil which has the smaller resistance is increased over the initial current. In order not to have large current value than the initial value, the smaller difference value between R_1 and R_2 is preferable.

3.4 Current Characteristic of No Dumping Coil in Case of Dumping of a Neighbouring Coil

The current characteristic of no dumping coil is here calculated on the case of dumping of a neighbouring coil in order to check the worst condition of no operation of circuit breaker. The current $I_1(t)$ of no dumping coil is shown by the following equation,

$$I_1(t) = \left(1 + \frac{M}{L}\right) \cdot I_1(0) - \frac{M}{L} \cdot I_2(0)e^{-\frac{R_2}{L} t}$$

where L/R_2 is the time constant of the neighbouring coil. If the time after the dumping is sufficiently long. The second term of the above equation diminishes.

A numerical value is presented here on the example of LCT test "ALT A" where the test coil of 110 % current is not dumped and a neighbour is dumped.

$$\begin{aligned} I_1(\infty) &= \left(1 + \frac{0.390}{2.141}\right) \times 11 \text{ kA} \\ &= 13 \text{ kA} \end{aligned}$$

If two neighbouring coils are dumped without opening of the circuit breaker of the test coil, the current value of the test coils is more than 13 kA. Such a high value is above the stable operational current calculated by thermal equation.²⁾ Consequently all six coil should be absolutely discharged in any quenching case.

4. Experimental Measurement of Breakdown Voltage in Coil Quenching

4.1 Insulating Configuration of the Japanese LCT Coil and ORNL Specification

In the Japanese LCT coil winding, the roughed surfaces of the conductor is separated with fiber reinforced plastics of 3 mm thickness for the purpose of electric insulation. On the other hand ORNL specification of insulation for LCT coil are summarized as follows.¹⁾

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- (1) The coil insulation resistance shall be a minimum of 100 k Ω between conductor and ground at 4.2 times the quench voltage dc when measured in air at ambient conditions.
- (2) The insulation resistance of layer-to-layer or pie-to-pie shall be a minimum of 100 k Ω when tested by applying a voltage of 4.2 times the voltage which will appear between adjacent layer or pies.
- (3) The coil shall withstand a potential of 3 times the voltage of quench rac, root-mean-square, 60 Hz, applied for one minute between the conductor and ground. This requirement shall be met for ambient conditions with the coolant volume filled with He gas at a pressure of 1 ± 0.1 atmosphere.

4.2 Experimental Procedure

The insulation model specimens simulating to pie-to-pie insulation, shown in Fig. 3 were set up in He dewar, a series of voltage breakdown test were carried out.

An appearance of the model and the roughed surface electrode are shown in Fig. 4. The FRP (fiber reinforced plastic) spacers with 3 mm thickness are used as insulators, and two kinds of cooling surface with smooth surface and roughed surface of THERMO EXCELL³⁾ (commercially named) are used as electrodes.

The surfaces of spacers were polished by emery paper before setting up into the electrodes. In the experiments two types of voltage DC (+,-) and AC rms (50 Hz) are applied. Breakdown in any case arose on the surface of FRP spacer. The voltage is applied between conductor models in 4.2 K Liq, He, 4.2 K Gas He, room temperature Gas He and room temperature Air. The model specimen in 4.2 K Gas He is prepared such that the level of Liq He is at the center of spacer insulating vertical channel.

In order to investigate breakdown voltage in the condition of boiling He, the Liq He was heated up with a 100 W heater in the bottom of the model specimen. Thus He bubbles were floating up in the insulating channel and in this condition a voltage was applied between conductors. Photographs of the experiment with and without heating are presented in Fig. 5(a) and 5(b) respectively.

4.3 Experimental Results

The experimental results of breakdown voltage tests are summarized in Table 3.

Main conclusions of the breakdown voltage tests are followings.

- (1) THERMO EXCELL surface decreases 50 % of the flashover voltage of FRP spacer in comparison with that of smooth cooling surface in 4.2 K Gas He.
- (2) The flashover voltage of 3 mm thickness spacer in 4.2 K He is at least DC 10 kV, which has large clearance for the quenching voltage 1 kV/20 layers i.e. 50 V.
- (3) The insulating strength in Liq He of 3 mm thickness spacer is about DC 20 kV.
- (4) Boiling of He decreases the insulating strength in Liq He, but the insulating strength with boiling He is considerably higher than that of Gas He. (dielectric constant ϵ in Liq He = 1.049)
- (5) The rms of AC breakdown voltage is in any case in this experiment about 50 % of DC breakdown voltage.
- (6) The value of scattering in AC breakdown voltage is smaller than that in DC breakdown voltage.
- (7) On the insulating configuration it would be noticeable that the breakdown voltage in Gas He is extremely low at the room temperature.

5. Temperature Rise of Conductor due to Coil Quenching

5.1 Temperature Rise in the Case where the Whole Conductor is changed into Normal State

In the case where whole length of winding is changed into normal stage, the energy dissipation in the winding with the external resistance 0.1Ω is as following.

$$196.8 \times 10^6 \text{ J} \times \frac{0.0294 \Omega}{0.1 \Omega + 0.0294 \Omega} = 44.71 \times 10^6 \text{ J}$$

In the above calculation the constant value of substrate resistance at 77 K is applied. For simplicity it is assumed that the whole energy is exhausted only in the winding.

The energy consumption per unit weight of winding is

$$(44.71 \times 10^6) \text{ J} \div (20.9 \times 10^3) \text{ kg} = 2139 \text{ J/kg.}$$

From the enthalpy of copper the temperature rise is 56 K.

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In such a way the temperature rise of each extended test is calculated and summarized in Table 4.

5.2 Hot Spot Temperature of Conductor with Fixed Cold Ends

During the resistive voltage across the coil terminals at coil quenching is lower than the detection voltage, the circuit breaker for protection does not operate.

When a comparatively short normal zone is limited and temperature rise is progressive, there may be an excess temperature rise of conductor by insufficiency of the generating voltage.

In fact such conditions are most probable when a short normal zone is limited by both cold ends with enough replenishment of liquid He.

The temperature of a conductor are calculated with the one-dimensional heat conduction equation (10).

$$m \cdot C(T) \cdot \frac{\partial T}{\partial t} = \frac{\partial}{\partial x} \left\{ \lambda(T) \cdot \frac{\partial T}{\partial x} \right\} + Q - \frac{P}{A} H \quad (10)$$

$$Q = \rho(T) \cdot \left\{ \frac{I(t)}{A} \right\}^2$$

$$H = 0 \quad (|x| \leq \ell/2)$$

$$T = 4.2 \text{ K} \quad (|x| \geq \ell/2)$$

where

- T : Temperature of conductor at the point (x,t)
- x : Coordinate of situation along conductor length
- t : Coordinate of time
- ρ : Specific resistivity of copper
- C : Specific heat of copper
- λ : Heat conductivity of copper
- Q : Heat generation rate by current
- H : Heat dissipation factor
- P : Periphery of conductor section
- A : Section area of conductor
- I : Current of conductor
- ℓ : Dry zone length
- m : Specific gravity of conductor

For simplicity the next conditions are assumed in order to keep the estimation safe.

- (1) A dry zone of conductor is due to vapor locking etc.
- (2) Enough replenishment of liquid He prevents dry zone length from progressing.
- (3) Enough replenishment of liquid He keeps the both ends of the dry zone at the constant temperature of 4.2 K.
- (4) There is no heat dissipation from surface of the dry zone conductor.

The main parameters of the Japanese LCT coil are shown in Table 2.

Then calculation procedure with Crank-Nicolson method and the computer code are written in the Appendix.

The calculated results are given in Table 5 and in Fig. 6. If the dry zone length is less than 0.7 m, the temperature is saturated without detection of which voltage is 80 mV. The hot spot temperature reached at the maximum value when the dry zone length is 0.7 m, and it is 165 K. Figure 7 shows an example of the temperature distribution along the conductor of dry zone of 0.8 m in length. As conclusion in this section it can be said that the maximum temperature rise is attained to across the conductor length of 0.7 m, so that there is no anxiety of thermal stress in the winding.

6. Conclusion

Several electric problems due to quenching of the Japanese LCT coil are picked up and examined by calculation and experiment.

The conclusions of this report are listed as followings.

- (1) The protection resistance 0.1Ω of the Japanese LCT coil is chosen in view of the voltage below 1 kV and the temperature rise below 80 K at coil quenching.
- (2) The analysis of current dumping with six coil system proves that the whole coils should be simultaneously dumped at quenching of any coil with the condition of equivalent resistance value.
- (3) The insulating strength in the winding with rough surface in the Japanese LCT coil has enough margin for practical quenching voltage.
- (4) The temperature rise of the Japanese LCT coil at quenching is calculated as 60 K in the case where the whole winding is normalized, and as 165 K in the case where local winding is normalized.

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Acknowledgement

The participation of the staffs of Superconducting Magnet Laboratory to the discussion is hereby acknowledged.

Reference

- 1) UCC-ND; Technical Specification No. TS14700-01 (Nov. 1976).
- 2) S. Shimamoto, et al.; Japanese Design of a Test Coil for the Large Coil Task, Paper to 8th Symp. on Engineering Problems of Fusion Research (Nov. 1979).
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Table 1 Main Parameters of the Japanese LCT Coil

Item	Value
Coil Bore	2.5 m × 3.5 m
Maximum Operational Field	8.0 T
Ampere Turns	6.76×10^6 AT
Operational Current	10.21 kA
S.C. Material	Nb-Ti
Conductor	Rough Surface Copper Stabilizer Soldered Cable Superconductor
Winding	Edge Wise, 2 Grading 20 Double Pancake
Weight	39 ~ 40 ton

Table 2 Electric Parameters of the Japanese LCT Coil

Item	Value
Coil Winding Weight	20.9 ton
Substrate Resistance	0.0133 Ω at 4.2 K (6×10^{-10} Ω m)
	0.0294 Ω at 77 K (13.3×10^{-10} Ω m)
Inductance	$L_0 = 2.141$ H
	$M_1 = 0.390$ H (No.1 - No.2)
	$M_2 = 0.129$ H (No.1 - No.3)
	$M_3 = 0.084$ H (No.1 - No.4)
Conductor Current	100 % = 10 kA

Table 3 FRP Flashover Voltage ; 3 mm, 1 atm

Insulating Media	Temp.	THERMO EXCELL C*		Smoothed surface	
		DC	AC rms	DC	AC rms
Liq He	4.2 K	19.8 kV	10.1 kV	20 kV	11.6 kV
Boiling He in Liq He	4.2 K	15.1	8.9	20	11.6
Gas He	4.2 K	10.8	4.8	19.7	9.4
Gas He	15 °C	1.08	0.59	1.16	0.6
Air	15 °C	5.24	3.12	9.98	4.16

* Height of saw-teeth : 1.2 mm, Interval of saw-teeth: 0.8 mm

Table 4 Magnetic Energy of No.1 Coil and
Temperature Rise of ORNL Test Sequences

Test	I ₁	I ₂	I ₃	I ₄	I ₅	I ₆	E ₁	Temperature Rise
Normal Op.	100 %	80 %	80 %	80 %	80 %	80 %	196.8 MJ	56 K
ALT A	110 %	90 %	90 %	90 %	90 %	90 %	248.9 MJ	60 K
ALT B	100 %	100 %	100 %	100 %	100 %	0 %	210.8 MJ	57 K
ALT C	140 %	0 %	0 %	0 %	0 %	0 %	209.8 MJ	57 K

Table 5 Calculated Results

L (m)	T ₁ (K)	t ₁ (sec)	T _h (K)	t _h (sec)
0.1	---	---	6.56	0.06 ~
0.2	---	---	12.4	0.4 ~
0.4	---	---	48.5	42 ~
0.5	---	---	58.4	100 ~
0.6	---	---	88.2	650 ~
0.7	163.8	183.6	165.6	190
0.8	149.1	87.1	160.5	100
1.0	127.8	52.2	156.5	74
1.2	111.5	39.7	153.0	70
1.4	98.6	32.4	148.3	68
1.5	93.7	30.0	146.1	70
1.6	89.4	27.8	144.0	70
1.8	80.0	23.2	136.4	72
2.0	74.5	20.7	133.3	76

L ; Dry Zone Length

T₁; Temperature corresponding to V₁=80 mVt₁; Time corresponding to V₁=80 mVT_h; Maximum temperature over all timet_h; Time corresponding to maximum temperature

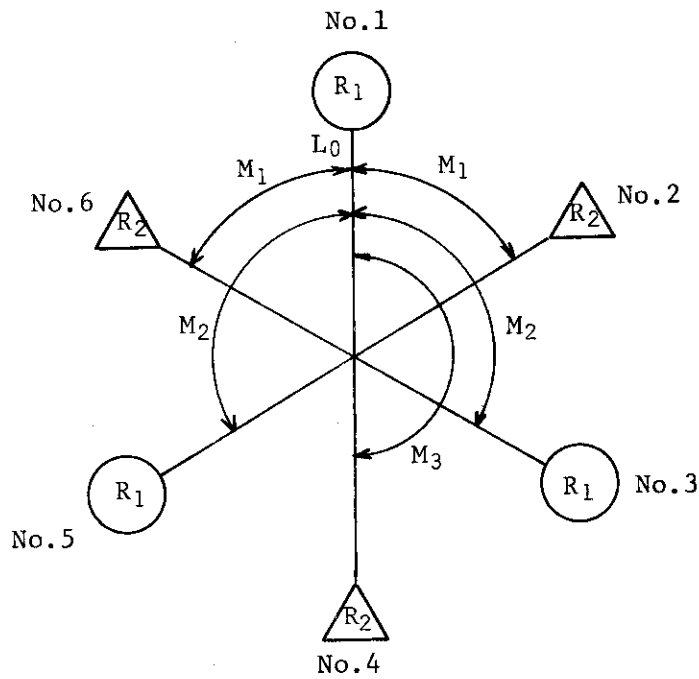


Fig. 1 Coil Arrangement with Alternately Different Dumping Resistance

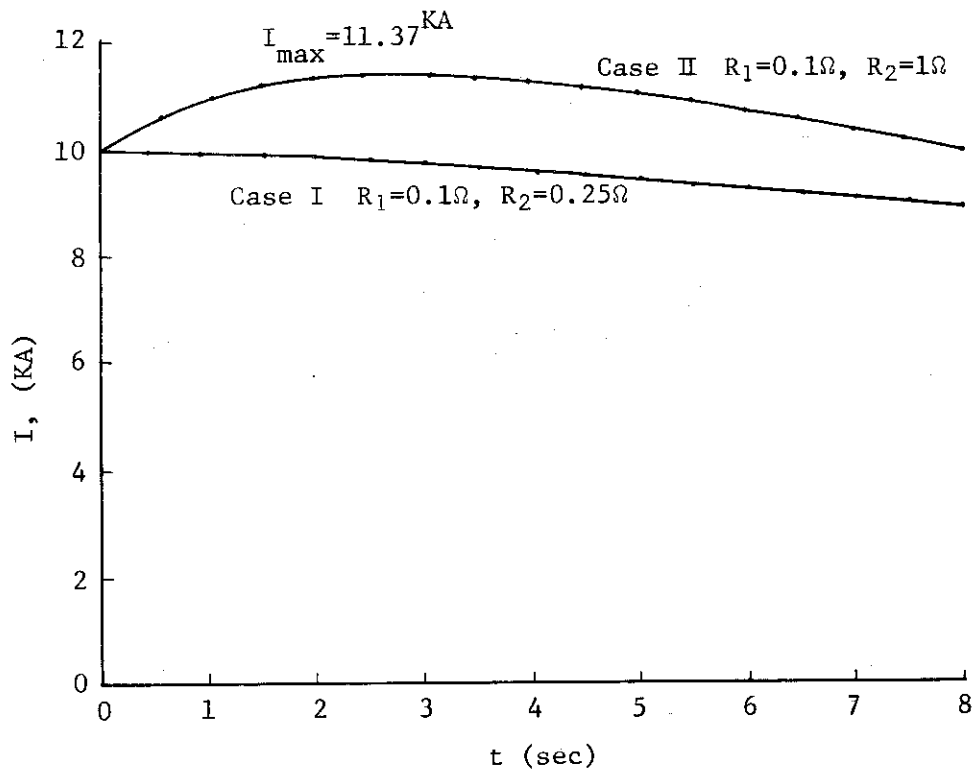


Fig. 2 Dumping Current Characteristics with Different Dumping Resistors

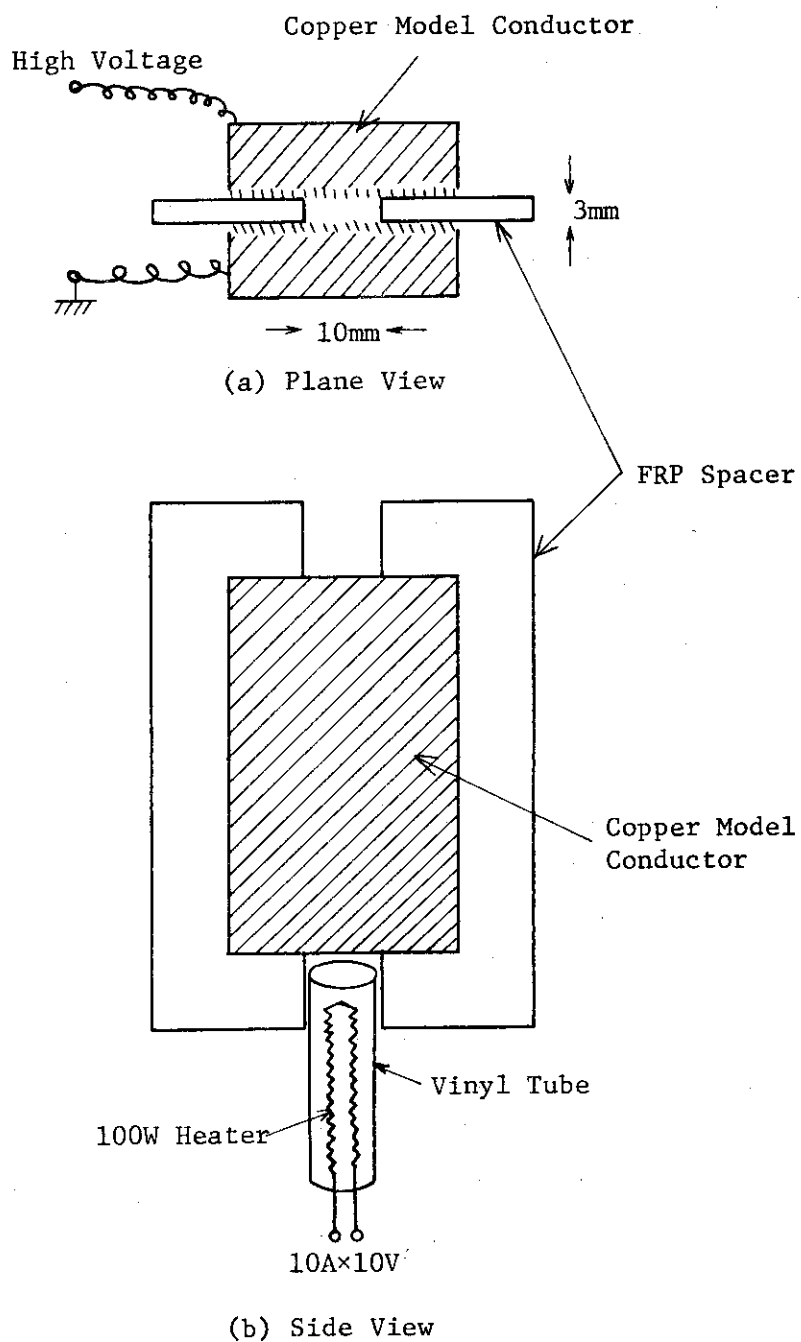
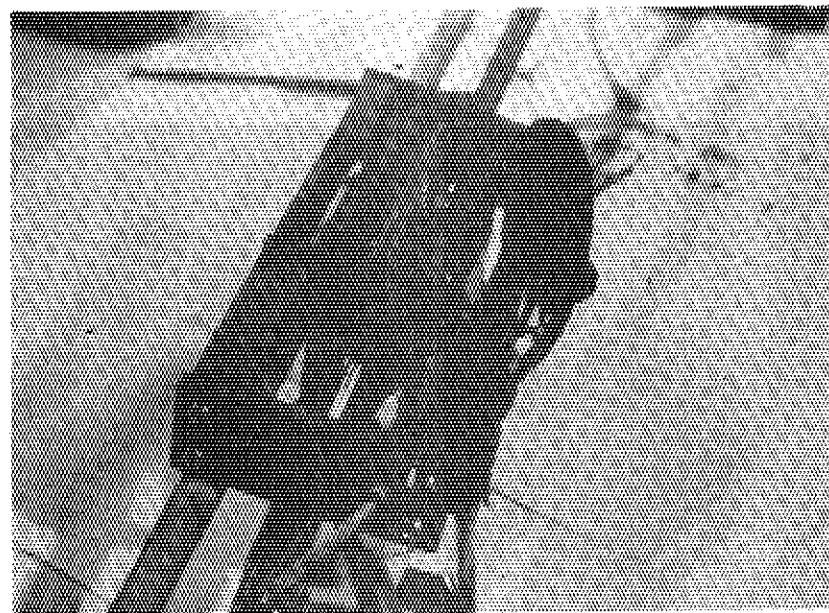
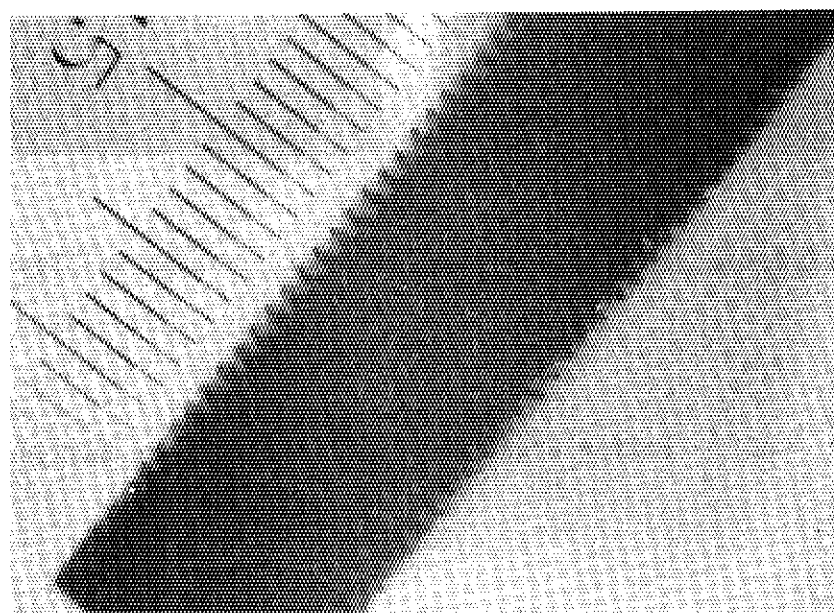


Fig. 3 Configuration of Test Sample

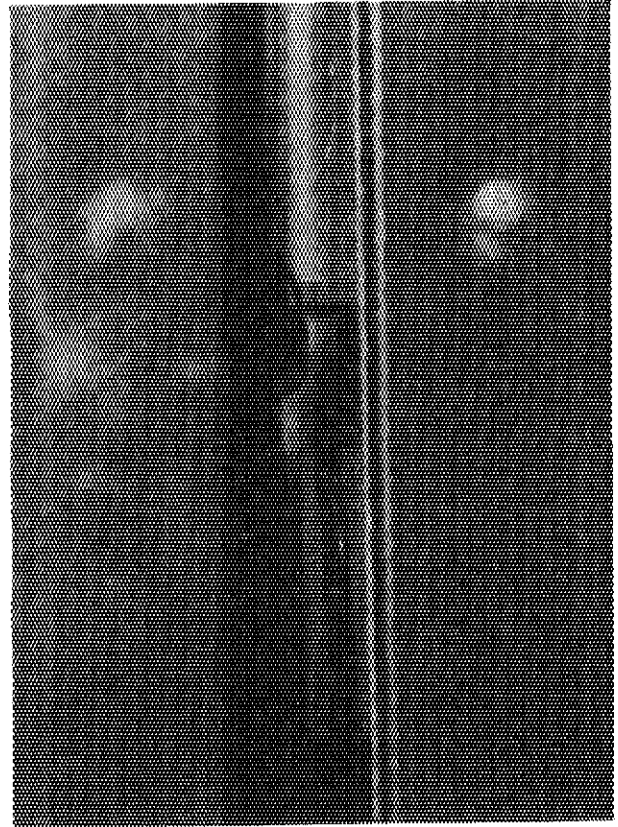
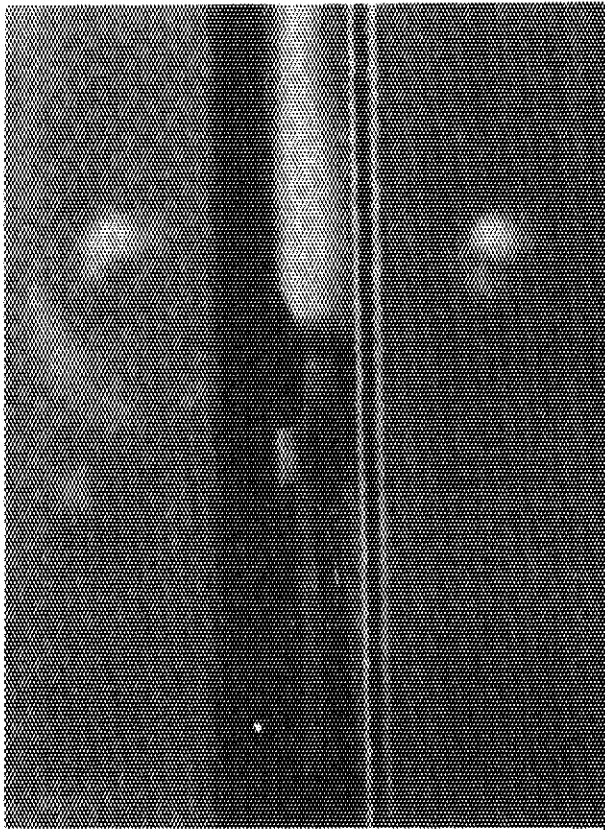


(a) Sample and Sample Holder



(b) Section View of THERMOEXCELL Surface

Fig. 4 Sample of Breakdown Voltage Test



(a) Helium bubbles in Liquid Helium (b) No bubbling in Liquid Helium

Fig. 5 Helium Conditions with and without Bubbles

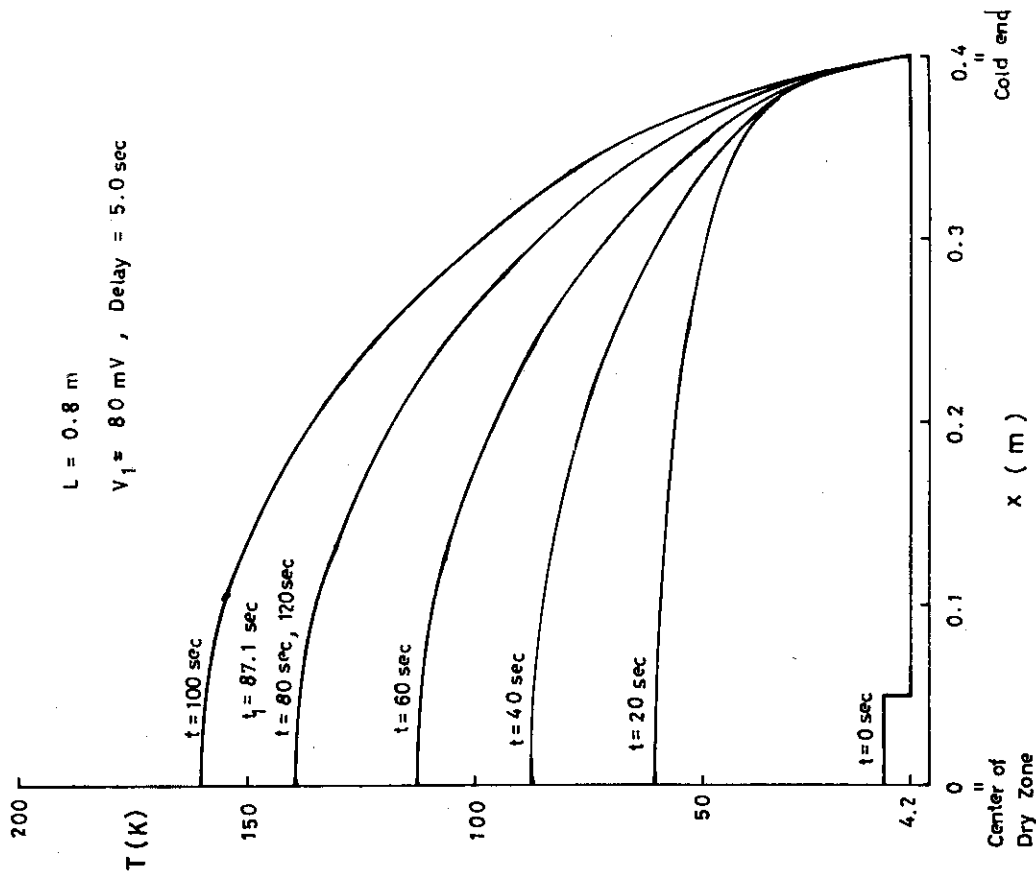


Fig. 7 Temperature Distribution along a Conductor by 0.8 m Dry Zone Length

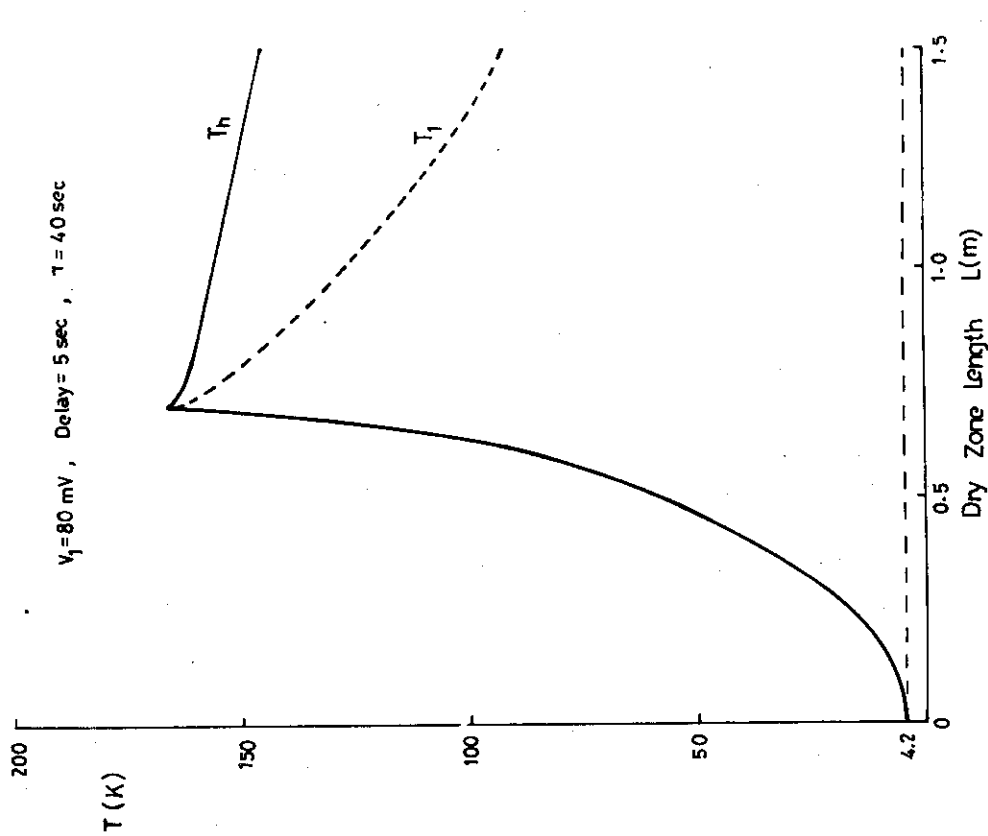


Fig. 6 Maximum Temperature in Relation with Dry Zone Length

Appendix Computer Code for Calculation of Hot Spot Temperature of Conductor due to Coil Quenching

The differential equation (10) is transferred to the difference equation (11) with Crank-Nicolson method.

$$\begin{aligned} \frac{m \cdot C(T)}{\Delta t} (u_{i,j+1} - u_{i,j}) = & \frac{1}{2} \{ \lambda(T) \cdot \frac{u_{i-1,j+1} - 2u_{i,j+1} + u_{i+1,j+1}}{\Delta x^2} \\ & + \lambda(T) \cdot \frac{u_{i-1,j} - 2u_{i,j} + u_{i+1,j}}{\Delta x^2} \} \\ & + \frac{1}{4} \cdot \frac{\partial \lambda(T)}{\partial x} \left\{ \frac{u_{i+1,j+1} - u_{i-1,j+1}}{\Delta x} + \frac{u_{i+1,j} - u_{i-1,j}}{\Delta x} \right\} \\ & + Q(T) - \frac{P}{A} H(T,x) \end{aligned} \quad (11)$$

$u_{i,j}$, $i \cdot \Delta x$ and $j \cdot \Delta t$ in the equation (10) are respectively $T(x,t)$, x and t in the equation (11).

Now $Q(T)$ is generated by the current which is constant until that the terminal voltage of the coil is below the detection voltage V_1 and dumped with the dumping time constant τ after a delay time t_1 .

Furthermore the equation (11) is transformed to the gradualizing expressions in the code.

In that code the symbols concerning "IN PUT" are as followings, and numerics are used in MKS unit.

DX; x , HFLG; l ; Dry zone length, DSEC; Δt , FTIME; Calculated last time,

AREA: A , PEFF; P , CUR; $I(0)$, GRAV; m ,

IP; Full mesh number of initial dry zone length

IS; Spaced mesh number for recording the solution along the dry zone length

IKM; Division number for recording the solution along the dry zone length

SECS; Spaced time for recording the solution



INPUT DATA SHEET

PAGE OF

氏名	H 付		プログラム名		JOB NO.		カード色指定		PUNCH	
	1	2	3	4	5	6	7	8	9	0
所屬	電 話		研究テーマ番号		IBJOB DECKNAME		備 考		73-80	
1	2	3	4	5	6	7	8	9	0	YES <input type="checkbox"/>
2	3	4	5	6	7	8	9	0	1	NO <input type="checkbox"/>
0.01	0.3	HFLG	DSEC	FTIME	AREA	PEFF	CUR			
1	3			10.0						
IP	IS		IKM	SECS						
1	2									
2	3									
3	4									
4	5									
5	6									
6	7									
7	8									
8	9									
9	0									
0	1									
1	2									
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5	6									
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7	8									
8	9									
9	0									
0	1									
1	2									
2	3									
3	4									
4	5									
5	6									
6	7									
7	8									
8	9									
9	0									

* 73-75 : DATAID / 76-80 : SEQUENTIAL NUMBER

共通E173

ISN	ST-NO	SOURCE PROGRAM	SEQUENCE
	C	CHOUDENDOU K.OKA: 1979.10.2, TEMP DSTRIBUTION ALONG CONDUCTOR	
1		DIMENSION UA(1000),UB(1000),TMP(1000),UU(1000),A(1000),B(1000),	
2		IC(1000),D(1000),ALPH(1000),SK(1000)	
3		DIMENSION ALTT(10),RHOD(10),HNTT(10),CCUU(10)	
4		DIMENSION DLTX(10),SAMEN(10),UHEN(10)	
5		READ (5,1001) DX,HFLG, DSEC,FTIME,AREA,PEFF,CUR,GRAV	
6	1001	FORMAT(9F10.0)	
7		READ (5,1002) IP,IS,IKM,SECS	
8	1002	FORMAT(3I10,F10.0)	
9		SECP=SECS	
10		BJ=0.0	
11		HEATM=14000.0	
12		TB=4.2+1.2	
13		DET=TS=4.2	
14		X=IP+DX	
15		DX2=DX**2	
16		VDX2=2.0*DX**2	
17		VDESEC=2.0*DSEC	
18		WDX=4.0*DX	
19		IM=HFLG/DX	
20		IKM=IM/IS	
21		JM=FTIME/DSEC	
22		CA=(CUR/AREA)**2	
23		PA=PEFF/AREA	
24	2000	WRITE(6,2000) DX,HFLG,DSEC,FTIME,AREA,PEFF,CUR,PA	
25		FORMAT(7H,3A,4DHX,HFLG,DSEC,FTIME,AREA,PEFF,CUR,PA	
26	2009	FORMAT(7H,3A,4DHCA,GRAV,IM,JM,IP,IS,IKM,SECS	
27		1BE11.4)	
28		DO 25 I=1,IM	
29		IF(I.GT.IP) GO TO 26	
30		UA(I)=0.0	
31		GO TO 27	
32		27 CONTINUE	
33		25 CONTINUE	
34		UAZ=UA(I)	
35		DO 15 IK=1,IKM	
36		J=IS*IK	
37		15 UJ(IK)=UA(I)	
38		WRITE(6,2001)	
39	2001	FORMAT(7H,3A,30HINITIAL CONDISION (0.0 SEC) ,)	
40		WRITE(6,2002) UAZ,OHJ(IK),IK=1,IKM	
41	2002	FORMAT(7H,3A,11F11.4)	
42		J=0	
43		5 CONTINUE	
44		DO 20 I=1,IM	
45		20 TMP(I)=JA(I)	
46		I=1	
47		Z=1	
48		X=Z*DX	
49		T1=UAZ	
50		T2=LA(2)	
51		T=UA(I)	
52		ALTT(I)=T	
53		AL12=AL(T2)	

ISN	ST-NO	SOURCE PROGRAM (F MAIN)	SEQUENCE
54		AL1=AL(T1)	
55		DALXT=(AL12-AL1)/(2.0*DX)	
56		WT=CA*RHO(T)	
57		IF(X.GT.XP) GO TO 40	
58		HT=0.0	
59		GO TO 42	
60		40 HT=(I)	
61	42	CONTINUE	
62		D(I)=AL1/VDX2 *CUA(2)=2.0*UA(I)+UAZ)+DALXT/WDX*CUA(2)-UAZ)+BT	
63		1=PA*HT+GRAV*CCU(T)/DSEC*UA(I)	
64		A(I)=AL1/VDX2-DALXT/WDX	
65		C(I)=AL1/VDX2+DALXT/WDX	
66		B(I)=GRAV*CCU(T)/DSEC*AL1/DX2	
67		S(I)=D(I)	
68		ALPH(I)=B(I)-A(I)	
69		CCUU(I)=CCU(T)	
70		ALTT(I)=AL1	
71		RHO(I)=RHO(T)	
72		HNTT(I)=HT	
73		DLTX(I)=DALXT	
74		DO 30 I=2,IM-1	
75		Z=I	
76		X=Z*DX	
77		T1=UA(I-1)	
78		T2=UA(I+1)	
79		T=UA(I)	
80		AL1=AL(T)	
81		AL12=AL(T2)	
82		AL12=AL(T2)	
83		DALXT=(AL12-AL1)/(2.0*DX)	
84		WT=CA*RHO(T)	
85		IF(X.GT.XP) GO TO 50	
86		HT=0.0	
87		GO TO 52	
88		50 HT=(I)	
89		52 CONTINUE	
90		D(I)=AL1/VDX2 *CUA(2)=2.0*UA(I)+UAZ)+DALXT/WDX*CUA(2)-UAZ)+BT	
91		1=PA*HT+GRAV*CCU(T)/DSEC*UA(I)	
92		A(I)=AL1/VDX2-DALXT/WDX	
93		C(I)=AL1/VDX2+DALXT/WDX	
94		B(I)=GRAV*CCU(T)/DSEC*AL1/DX2	
95		ALPH(I)=B(I)-A(I)+C(I-1)/ALPH(I-1)	
96		S(I)=D(I)+A(I)*S(I-1)/ALPH(I-1)	
97		IF(I.GT.2) GO TO 91	
98		IF(I.GT.9) GO TO 91	
99		DLTX(I)=DALXT	
100		CCUU(I)=CCU(T)	
101		ALTT(I)=AL1	
102		RHO(I)=RHO(T)	
103		HNTT(I)=HT	
104	91	CONTINUE	
105	30	CONTINUE	
106		UB(IM)=4.2	
107		DO 33 I=1,IM-1	
108		33 UB(I)=C(I)+C(I)*UB(I+1)/ALPH(I)	

```

ISN  ST-NO      SOURCE PROGRAM      ( FTMAIN )      SEQUENCE
109          CONTINUE
110          UB2=UB(1)
111          IF (J.GT.2) GO TO 92
112          DO 37 I=2,9
113          SAHEN(1)=GRAV*CCUU(1)/DSEC*(UB(1)-UA(1))
114          UHENE(1)=ALTT(1)/VDX*(UB(1)-2.0*UB(1)+UB(1+1)+UA(1+1)-2.0*UA(1)
          1*UA(1-1)+DLTX(1)/VDX*(UB(1-1)-UB(1-1)+UA(1+1)-UA(1-1))
          2*CA*RHOD(1)-PA*HHTT(1)
115          37 CONTINUE
116          SAHEN(1)=GRAV*CCUU(1)/DSEC*(UB(1)-UA(1))
117          UHENE(1)=ALTT(1)/VDX*(UB(2)+UB(1)+UB(1)+UB(2)-2.0*UA(1)+UA(2)
          2*DLTX(1)/VDX*(UB(2)-UB(2)+UA(2)+CA*RHOD(1)-PA*HHTT(1)
118          92 CONTINUE
119          J=J+1
120          PJ=J
121          SEC=DSEC*PJ
122          IF (J.GT.3) GO TO 93
123          WRITE(6,2004) SEC
124          WRITE(6,2005) UAZ,(UA(I),I=1,10)
125          WRITE(6,5001) (A(I),I=1,9)
126          WRITE(6,5001) (B(I),I=1,9)
127          WRITE(6,5001) (C(I),I=1,9)
128          WRITE(6,5001) (D(I),I=1,9)
129          WRITE(6,5001) (E(I),I=1,9)
130          WRITE(6,5001) (ALPH(I),I=1,9)
131          WRITE(6,5001) (CCUU(I),I=1,9)
132          WRITE(6,5001) (ALTT(I),I=1,9)
133          WRITE(6,5001) (RHOD(I),I=1,9)
134          WRITE(6,5001) (HHTT(I),I=1,9)
135          WRITE(6,5001) (SAHEN(I),I=1,9)
136          WRITE(6,5001) (UHENE(I),I=1,9)
137          5001 FORMAT(1H,1X,10E11.4)
138          WRITE(6,2005) UBZ,(UB(I),I=1,10)
139          93 CONTINUE
140          IF (SEC.GE.1.0) GO TO 300
141          GO TO 309
142          300 CONTINUE
143          SJ=J+1.0
144          SECP=SJ*SECS
145          DO 16 IK=1,IKM
146          K=IS*(K
147          16 UU(K)=UB(K)
148          WRITE(6,2004) SEC
149          2004 FORMAT(1H,1X,F8.3)
150          WRITE(6,2005) UBZ,(UU(K),K=1,IKM)
151          2005 FORMAT(1H,3X,11E11.4)
152          309 CONTINUE
153          IF (J.GT.10) GO TO 6
154          DO 34 I=1,IM
155          34 UA(I)=UB(I)
156          UAZ=UBZ
157          GO TO 5
158          6 CONTINUE
159          STOP
160          END
    
```

```

ISN  ST-NO      SOURCE PROGRAM      SEQUENCE
C    CCU(T) : (J/K/G/X) : R=(AL(T)/DX**2)/(GRAV*CCU(T)/DSEC)
1    FUNCTION CCU(T)
2    IF (T.GT.40.0) GO TO 601
3    CCU = 0.95312E-3*T**3
4    GO TO 609
5    601 IF (T.GT.80.0) GO TO 602
6    CCU = 3.6*(T-40.0)+61.0
7    GO TO 609
8    602 IF (T.GT.100.0) GO TO 603
9    CCU = 2.45*T+9.0
10   GO TO 609
11   603 IF (T.GT.150.0) GO TO 604
12   CCU = 1.12*T+142.0
13   GO TO 609
14   604 IF (T.GT.200.0) GO TO 605
15   CCU = 0.42*T+247.0
16   GO TO 609
17   605 CCU = 0.38*T+255.0
18   609 CONTINUE
19   RETURN
20   END
    
```

```

ISN  ST-NO      SOURCE PROGRAM      SEQUENCE
C    AL(T) : (W/M/K)
1    FUNCTION AL(T)
2    AL=78.77*T+0.58
3    RETURN
4    END
    
```

```

ISN  ST-NO      SOURCE PROGRAM      SEQUENCE
C    RHO(T) : (OH**M)
1    FUNCTION RHO(T)
2    RHO = 0.0
3    IF (T.GT.5.8) GO TO 700
4    GO TO 709
5    700 IF (T.GT.80.0) GO TO 701
6    RHO = 4.66E-15*T**3+6.0E-10
7    GO TO 709
8    701 RHO = 0.7E-10*(T-50.0)+6.0E-10
9    709 CONTINUE
10   RETURN
11   END
    
```

```

ISN  ST-NO      SOURCE PROGRAM      SEQUENCE
C    H(T) : (W/M2)
1    FUNCTION H(T)
2    H = 0.0
3    809 CONTINUE
4    RETURN
5    END
    
```